Course Summary: Grade 2 mathematics is about (1) extending understanding of base-ten notation; (2) building fluency with addition and subtraction; (3) using standard units of measure; and (4) describing and analyzing shapes.

- 1. Make sense of problems and persevere in solving them.
 - 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
 - 4. Model with mathematics.
 - 5. Use appropriate tools strategically.
 - 6. Attend to precision.
 - 7. Look for and make use of structure.
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Unit of Study	Unit 1 - Sums and Differences to 100
Time Frame/Pacing	10 days
Time Trame/Tacing	Notes on Pacing: None for this module
Big Ideas	Mathematical relationships can be represented as expressions, equations, and inequalities in mathematical situations.
Unit Essential Questions	How do place value understanding and properties of operations contribute to solving addition and subtraction problems?
	How do you represent and solve problems involving addition and subtraction?
	Can you demonstrate addition and subtraction fluently within 20?
	 How can expressions, equations, and inequalities be used to quantify, solve, model and/or analyze mathematical situations?
PA Core Standards	CC.2.2.A.1 Represent and solve problems involving addition and subtraction within 100.
	CC.2.2.A.2 Use mental strategies to add and subtract within 20.
	CC.2.1.2.B.3 Use place value understanding and properties of operations to add and
	subtract within 1000.
Learning Objectives	adding and subtracting within 20 and within 100
(Concepts Taught)	 solve addition and subtraction word problems
1 8 /	• use math drawings to represent each situation
Performance	Foundations for Fluency with Sums and Differences Within 100
Objectives	Practice making ten and adding to ten.
(Skills Demonstrated)	Practice making the next ten and adding to a multiple of ten.
,	Initiating Fluency with Addition and Subtraction Within 100
	Add and subtract like units.
	Make a ten to add within 20.
	Make a ten to add within 100.
	• Subtract single-digit numbers from multiples of 10 within 100.
	• Take from ten within 20.

	Take from ten within 100.
Key Vocabulary	New or Recently Introduced Terms
	Addend
	Familiar Terms and Symbols
	Sum (PA Core Math Vocab), a ten, count on, expression, like units, make ten and
	take from ten, number sentence, equation (PA Core Vocab), number bond, a one,
	part,
	partners to 10, "Say Ten" counting, ten plus facts, total
Assessments	Exit tickets for all lessons, End of Module Assessment
	Topic A quiz: https://embarc.online/mod/page/view.php?id=8343
	Topic B quiz: https://embarc.online/mod/page/view.php?id=8344
Authentic Examples	Application Problems
(real-world tasks)	Friends You Can Count On, Level A and B
Visual	100 bead Rekenrek
Representations and	 number bonds
Strategies	• 5 group column
Ü	• whiteboards
	• dice
	place value chart
	Hide Zero cards
	• quick ten
	• linking cubes
	• ten frame cards
Writing in Math	End of Module Assessment Questions 2 and 4. Write a statement to answer the
8	question (pp. 110- 11 in Teacher Edition).
Culturally Responsive	Lesson 7 Application Problem
Activities	• https://www.engageny.org/resource/grade-2-mathematics-module-1 (see the
	various language resources under "Downloadable Resources")
	Mayan Mathematics
	http://www.michielb.nl/maya/math.html (compare quick tens and ones with the
	Mayan representation of numbers)
Resources and	Primary Resource: Eureka Module1
Differentiation Tools	Other Resources:
	• <u>www.zearn.org</u> (Grade 2 Mission 1)
	Number Talks
	Hundreds Chart
	• Ten frames
	Number Lines
	• 3-Act Math Task: https://gfletchy.com/the-whopper-jar/
	• Problem of the Month: <u>Calculating Palindromes</u> ,
	o Friends You Can Count On, Level A and B
	o <u>Got Your Number</u> , Level A
	o <u>Party Time</u>
	• Illustrative Mathematics: https://tasks.illustrativemathematics.org/2.OA.A ,
	https://tasks.illustrativemathematics.org/2.OA.B
	ELL Overlay for Listening and Reading Grades 1 and 2 Mathematics
	ELL Overlay for Speaking and Writing for Grades 1 and 2 Mathematics

Grade Level DOK	Grade 2 Math DOK Samples
Examples	

Course Summary: Grade 2 mathematics is about (1) extending understanding of base-ten notation; (2) building fluency with addition and subtraction; (3) using standard units of measure; and (4) describing and analyzing shapes.

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Unit of Study	Unit 2 - Addition and Subtraction of Length Units
Time Frame/Pacing	12 days Notes on Pacing: consider consolidating Lessons 2 and 3, Lessons 4 and 5, and omitting Lesson 8 (see p. 3 of Teacher Manual)
Big Ideas	Measurement attributes can be quantified and estimated using customary and non-customary units of measure.
Unit Essential Questions	 How do we use units of measurement? How precise do measurements and calculations need to be?
PA Core Standards	CC.2.4.2.A.1 Measure and estimate lengths in standard units using appropriate tools. CC.2.4.2.A.6 Extend the concepts of addition and subtraction to problems involving length.
Learning Objectives (Concepts Taught)	 measure and estimate using standard units for length and solve measurement problems involving addition and subtraction of length and comparison use measurement tools with the understanding that linear measure involves an iteration (repetition) of units and that the smaller a unit, the more iterations (repetitions) are necessary to cover a given length metric units (centimeters and meters) to support upcoming work with place value concepts. learn the meaning of a length unit solve word problems involving addition and subtraction comparison situations
Performance Objectives	 Understand Concepts About the Ruler Connect measurement with physical units by using multiple Use iteration with one physical unit to measure.

(Skills Demonstrated)	Apply concepts to create unit rulers and measure lengths using
	 Measure and Estimate Length Using Different Measurement Tools Measure various objects using centimeter rulers and meter Develop estimation strategies by applying prior knowledge Measure and Compare Lengths Using Different Length Units Measure and compare lengths using centimeters and meters. Measure and compare lengths using standard metric length units and non-standard length units; relate measurement to unit size. Relate Addition and Subtraction to Length Solve addition and subtraction word problems using the ruler as a number line. Measure lengths of string using measurement tools, and use tape diagrams to represent and compare the lengths. Apply conceptual understanding of measurement by solving two-step word problems.
Key Vocabulary	New or Recently Introduced Terms benchmark, endpoint, estimate, hash mark, meter, meter stick or strip, number line, overlap, ruler Familiar Terms and Symbols centimeter, combine, compare, difference, height, length, length unit
Assessments	 Exit Tickets after each Lesson and End of Module Assessment Topic A quiz: https://embarc.online/mod/page/view.php?id=8623 Topic B and C quiz: https://embarc.online/mod/page/view.php?id=8624 Topic D quiz: https://embarc.online/mod/page/view.php?id=8626
Authentic Examples (real-world tasks)	 Application Problems Lessons 4 and 6 – measuring items with a centimeter ruler or meter stick Lesson 9 – measuring body parts with measuring tape
Visual Representations and Strategies	 centimeter cubes centimeter rulers large and small paper clips meter sticks paper meter strips whiteboards tape diagram
Writing in Math	• End of Module Assessment Questions 2b- Explain your choice using words. 2d -Who won? How do you know?, and 4b - Explain why using words (pp. 128-129 Teacher Edition).

Culturally	Lesson 7 Application Problem
Responsive	• https://www.engageny.org/resource/grade-2-mathematics-module-2 (see the
Activities	various language resources under "Downloadable Resources")
Resources and	Primary Resource: Eureka Module 2
Differentiation Tools	
	Other Resources:
	• www.zearn.org (Grade 2 Mission 2)
	Number Talks
	• See p. 7 in the Teacher's Manual for "Scaffolds"
	• 3-Act Math Task: https://gfletchy.com/let-it-fly/
	• Problem of the Month (Level A):
	http://www.insidemathematics.org/assets/problems-of-the-month/miles%20of%
	20tiles.pdf
	• Illustrative Mathematics: https://tasks.illustrativemathematics.org/2.OA.B ,
	https://tasks.illustrativemathematics.org/2.MD.A,
	https://tasks.illustrativemathematics.org/content-standards/2/MD/A/3,
	https://tasks.illustrativemathematics.org/2.MD.B
	ELL Overlay for Listening and Reading Grades 1 and 2 Mathematics
	ELL Overlay for Speaking and Writing for Grades 1 and 2 Mathematics
Grade Level DOK	Grade 2 Math DOK Samples
Examples	•

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Unit of Study	Unit 3 - Place Value, Counting, and Comparison of Numbers to 1,000
Time Frame/Pacing	25 days
	Notes on Pacing : consider omitting lesson 10 and use as an extension instead and
	consolidating lessons 17 and 18 (see p. 3 in the Teacher's Manual)
Big Ideas	Mathematical relationships among numbers can be represented, compared, and communicated.
Unit Essential	How do place value understanding and properties of operations contribute to
Questions	solving addition and subtraction problems?
	• How is mathematics used to quantify, compare, represent, and model numbers?
PA Core Standards	CC.2.1.2.B.1 Use place value concepts to represent amounts of tens and ones and to
	compare three digit numbers.
	CC.2.1.2.B.2 Use place value concepts to read, write and skip count to 1000.
Learning Objectives	• extension of understanding of base ten notation and apply their understanding of
(Concepts Taught)	place value to count and compare numbers to 1,000
	 understanding of various models of place value units
Performance	Forming Base Ten Units of Ten, a Hundred, and a Thousand
Objectives (Skills	• Bundle and count ones, tens, and hundreds to 1,000.
Demonstrated)	Understanding Place Value Units of One, Ten, and a Hundred
	• Count up and down between 100 and 220 using ones and tens.
	• Count up and down between 90 and 1,000 using ones, tens, and hundreds.
	Three-Digit Numbers in Unit, Standard, Expanded, and Word Forms
	• Count up to 1,000 on the place value chart.
	• Write base ten three-digit numbers in unit form; show the value of each digit.
	 Write base ten numbers in expanded form.
	 Write, read, and relate base ten numbers in all forms.

Modeling Base Ten Numbers Within 1,000 with Money • Count the total value of \$1, \$10, and \$100 bills up to \$1,000. • Count from \$10 to \$1,000 on the place value chart and the empty number line. • Explore \$1,000. How many \$10 bills can we change for a thousand dollar bill? Modeling Numbers Within 1,000 with Place Value Disks • Count the total value of ones, tens, and hundreds with place value disks. • Change 10 ones for 1 ten, 10 tens for 1 hundred, and 10 hundreds for 1 thousand. • Read and write numbers within 1,000 after modeling with place value disks. • Model numbers with more than 9 ones or 9 tens; write in expanded, unit, standard, and word forms. • Explore a situation with more than 9 groups of ten. **Comparing Two Three-Digit Numbers** • Compare two three-digit numbers using <, >, and =. • Compare two three-digit numbers using <, >, and = when there are more than 9 ones or 9 tens. • Order numbers in different forms. (Optional) Finding 1, 10, and 100 More or Less than a Number • Model and use language to tell about 1 more and 1 less, 10 more and 10 less, and 100 more and 100 less. • Model 1 more and 1 less, 10 more and 10 less, and 100 more and 100 less when changing the hundreds place. • Complete a pattern counting up and down. **New or Recently Introduced Terms Key Vocabulary** base ten numerals, equivalent (PA Core Vocab), expanded form, hundreds place, one thousand (1,000), place value or number disk, standard form, unit form, word form **Familiar Terms and Symbols** =, <, and > (equal/is equal to, less than, and greater than), altogether, bundling/grouping, changing unknowns, how many more/less. how much more/less, more than/less than, number sentence, ones place, place value, renaming, tens place, units of ones/tens/hundreds/one thousand Assessments • Exit Tickets from each lesson, Mid-Module Assessment, End of Module Assessment Topic A and B quiz: https://embarc.online/mod/page/view.php?id=6762 • Topic C quiz: https://embarc.online/mod/page/view.php?id=6763 • Topic D quiz: https://embarc.online/mod/page/view.php?id=6764 • Topic E quiz: https://embarc.online/mod/page/view.php?id=6765 • Topic F quiz: https://embarc.online/mod/page/view.php?id=6766 • Topic G quiz: https://embarc.online/mod/page/view.php?id=6767 **Authentic Examples** • Application Problems (real-world tasks) • Lesson 8, 9, 10 – understanding place value through the use of bills Visual 2 boxes of 1,000 straws • clock number line Representations and Strategies Dice Dienes blocks • Hide Zero Cards • Hundreds place value chart

• meter strip
 Number spelling activity sheet
 place value box
• place value cards to 1,000
 place value disks
play money
 rubber bands
 small plastic bags
• whiteboards
Mid Madula Assessment question the a and d. Evaluin years an average avenue (n
Mid-Module Assessment question 1b, c, and d - Explain your answer using words (p. 149 Teacher Edition).
Lesson 21 Application Problem
• https://www.engageny.org/resource/grade-2-mathematics-module-3 (see the
various language resources under "Downloadable Resources")
Culturally Relevant Mathematics
See page 4 for place value tools from different cultures and historical time
periods.
Primary Resource: Eureka Module 3
Other Resources:
• www.zearn.org (Grade 2 Mission 3)
Number Talks
• See p. 9 "Scaffolds" in the Teacher's Manual
• 1,000 chart
• Illustrative Mathematics: https://tasks.illustrativemathematics.org/2.OA.B
ELL Overlay for Listening and Reading Grades 1 and 2 Mathematics
ELL Overlay for Speaking and Writing for Grades 1 and 2 Mathematics
Grade 2 Math DOK Samples

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Unit of Study	Unit 4 - Addition and Subtraction within 200 with Word Problems to 100
Time Frame/Pacing	35 days Notes on Pacing: consider omitting Lessons 29 and 30 (see p. 4 in the Teacher's Manual)
Big Ideas	Mathematical relationships can be represented as expressions, equations, and inequalities in mathematical situations.
Unit Essential Questions	 How do place value understanding and properties of operations contribute to solving addition and subtraction problems? How do you represent and solve problems involving addition and subtraction? Can you demonstrate addition and subtraction fluently within 20? How are relationships represented mathematically? How can expressions, equations, and inequalities be used to quantify, solve, model and/or analyze mathematical situations?
PA Core Standards	CC.2.2.2.A.1 Represent and solve problems involving addition and subtraction within 100. CC.2.1.2.B.3 Use place value understanding and properties of operations to add and subtract within 1000.
Learning Objectives (Concepts Taught)	 add and subtract within 200, moving from concrete to pictorial to abstract one-step and two-step word problems within 100
Performance Objectives (Skills Demonstrated)	 Sums and Differences Within 100 Relate 1 more, 1 less, 10 more, and 10 less to addition and subtraction of 1 and 10. Add and subtract multiples of 10 including counting on to subtract. Add and subtract multiples of 10 and some ones within 100.

• Solve one- and two-step word problems within 100 using strategies based on place value.

Strategies for Composing a Ten

- Use manipulatives to represent the composition of 10 ones as 1 ten with two-digit addends.
- Relate addition using manipulatives to a written vertical method.
- Use math drawings to represent the composition and relate drawings to a written method.
- Use math drawings to represent the composition when adding a two-digit to a three-digit addend.

Strategies for Decomposing a Ten

- Represent subtraction with and without the decomposition of 1 ten as 10 ones with manipulatives.
- Relate manipulative representations to a written method.
- Use math drawings to represent subtraction with and without decomposition and relate drawings to a written method.
- Represent subtraction with and without the decomposition when there is a three-digit minuend.
- Solve one- and two-step word problems within 100 using strategies based on place value.

Strategies for Composing Tens and Hundreds

- Use mental strategies to relate compositions of 10 tens as 1 hundred to 10 ones as 1 ten.
- Use manipulatives to represent additions with two compositions.
- Relate manipulative representations to a written method.
- Use math drawings to represent additions with up to two compositions and relate drawings to a written method.
- Solve additions with up to four addends with totals within 200 with and without two compositions of larger units.

Strategies for Decomposing Tens and Hundreds

- Use number bonds to break apart three-digit minuends and subtract from the hundred
- Use manipulatives to represent subtraction with decompositions of 1 hundred as 10 tens and 1 ten as 10 ones.
- Relate manipulative representations to a written method.
- Use math drawings to represent subtraction with up to two decompositions and relate drawings to a written method.
- Subtract from 200 and from numbers with zeros in the tens place.

Student Explanations of Written Methods

- Use and explain the totals below method using words, math drawings, and numbers.
- Compare totals below to new groups below as written methods.
- Solve two-step word problems within 100.

Key Vocabulary

New or Recently Introduced Terms

algorithm, compose, decompose, equation, new groups below, simplifying strategy, totals below

Familiar Terms and Symbols

addend, addition, bundle/unbundle/regroup/rename/change, difference, hundreds place,

	place value, subtraction, units of ones/tens/hundreds/thousands
Assessments	Exit Ticket from each lesson, Mid-Module Assessment, End of Module
	Assessment
	• Topic A quiz: https://embarc.online/mod/page/view.php?id=6780
	Topic B quiz: https://embarc.online/mod/page/view.php?id=6781
	• Topic C quiz: https://embarc.online/mod/page/view.php?id=6782
	• Topic D quiz: https://embarc.online/mod/page/view.php?id=6783
	• Topic E quiz: https://embarc.online/mod/page/view.php?id=6784
	• Topic F quiz: https://embarc.online/mod/page/view.php?id=6785
Authentic Examples	Application Problems
(real-world tasks)	 Lesson 31 – solving story problems with real world situations
Visual	arrow notation
Representations and	• chip model
Strategies	Hide Zero cards
_	 number bond
	whiteboards
	 place value charts
	 place value disks
	rekenrek
	tape diagram
Writing in Math	Mid Module Assessment question 4a - Explain why the strategy worked (p. 201
	Teacher Edition).
	End of Module Assessment question 4c - Explain your answer (pp. 406-307 Teacher's
	Edition).
Culturally	• Lesson 4, 6, 23, and 27 Application Problem
Responsive	• https://www.engageny.org/resource/grade-2-mathematics-module-4 (see the
Activities	various language resources under "Downloadable Resources")
Resources and	Primary Resource: Eureka Module 4
Differentiation	Other Resources:
Tools	• <u>www.zearn.org</u> (Grade 2 Mission 4)
	Number Talks
	• see p. 11 "Scaffolds" in the Teacher's Manual
	• Illustrative Mathematics: https://tasks.illustrativemathematics.org/2.OA.B ,
	https://tasks.illustrativemathematics.org/2.NBT.A
	ELL Overlay for Listening and Reading Grades 1 and 2 Mathematics
	ELL Overlay for Speaking and Writing for Grades 1 and 2 Mathematics
Grade Level DOK	Grade 2 Math DOK Samples
Examples	

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Unit of Study	Unit 5 - Foundations of Multiplication and Division
Time Frame	22 days Notes on Pacing: consider consolidating Lessons 1 and 2 and omitting Lessons 3, 8, and 11.
Big Ideas	 Mathematical relationships can be represented as expressions, equations, and inequalities in mathematical situations. Geometric relationships can be described, analyzed, and classified based on spatial reasoning and/or visualizations.
Unit Essential Questions	 Can you demonstrate how to work with equal groups of objects to gain foundations for multiplication? How can expressions, equations, and inequalities be used to quantify, solve, model, and/or analyze mathematical situations? How are spatial relationships, including shape and dimension, used to draw, construct, model, and represent real situations or solve problems?
PA Core Standards	CC.2.2.A.3 Work with equal groups of objects to gain foundations for multiplication. CC.2.3.2.A.1 Analyze and draw two- and three- dimensional shapes having specified attributes.
Learning Objectives (Concepts Taught)	 build the foundation for multiplication and division making equal groups where the unit is not ten relating the new unit to the one used to create it lays the foundation for multiplication
Performance Objectives (Skills Demonstrated)	Formation of Equal Groups Use manipulatives to create equal groups. Use math drawings to represent equal groups, and relate to repeated addition.

	 Represent equal groups with tape diagrams, and relate to repeated addition. Arrays and Equal Groups
	 Compose arrays from rows and columns, and count to find the total using objects.
	 Decompose arrays into rows and columns, and relate to repeated addition.
	Represent arrays and distinguish rows and columns using math drawings.
	 Create arrays using square tiles with gaps.
	 Solve word problems involving addition of equal groups in rows and columns.
	Rectangular Arrays as a Foundation for Multiplication and Division
	• Use square tiles to compose a rectangle, and relate to the array model.
	Use math drawings to compose a rectangle with square tiles.
	Use square tiles to decompose a rectangle. Use square tiles to decompose a rectangle.
	 Use scissors to partition a rectangle into same-size squares, and compose arrays with the squares.
	 Use math drawings to partition a rectangle with square tiles, and relate to repeated addition.
	 Use grid paper to create designs to develop spatial structuring. The Meaning of Even and Odd Numbers
	 Relate doubles to even numbers, and write number sentences to express the sums.
	 Pair objects and skip-count to relate to even numbers.
	• Investigate the pattern of even numbers: 0, 2, 4, 6, and 8 in the ones place, and relate to odd numbers.
	Use rectangular arrays to investigate odd and even numbers.
Key Vocabulary	New or Recently Introduced Terms
	array, columns, even number, odd number, repeated addition, rows, tessellation, whole number
	Familiar Terms and Symbols
	addends, doubles, equation, number path, number sentence, pair, rectangle,
	skip-counting
Assessments	Exit Tickets for each lesson, Mid Module Assessment, and End of Module
	Assessment
	• Topic A quiz: https://embarc.online/mod/page/view.php?id=6844
	• Topic B quiz: https://embarc.online/mod/page/view.php?id=6845
	 Topic C quiz: https://embarc.online/mod/page/view.php?id=6846 Topic D quiz: https://embarc.online/mod/page/view.php?id=6846
Authentic Examples	Application Problems
(real-world tasks)	1 ipplication 1 tooleins
Visual	• counters
Representations and	• number bond
Strategies	• number path
	• whiteboards
	• rectangular array
	• square tiles
Writing in Math	Lesson 18 Problem Set question 3. (pp. 243-244 Teacher Edition).
	Mid Module Assessment question 4b with student explanation (p. 163 Teacher
	Edition).

	End of Module Assessment question 5 (p. 273 Teacher Edition).
Culturally	https://www.engageny.org/resource/grade-2-mathematics-module-6 (see the
Culturally	1 00,000
Responsive	various language resources under "Downloadable Resources")
Activities	• Lesson 2 Application Problem, Lesson 9 Concept Development problems 1-3
Resources and	Primary Resource: Eureka Module 6
Differentiation Tools	Other Resources:
	• <u>www.zearn.org</u> (Grade 2 Mission 6)
	Number Talks
	• See p. 8 in the Teacher's Manual for "Scaffolds"
	Problem of the Month:
	• <u>Diminishing Return</u> , (Level A)
	• <u>Double Down</u> , (Level B)
	• Miles of Tiles, (Level A and B)
	 <u>Squirreling it Away</u>, (Level A and B)
	• the Wheel Shop (Level A and B)
	Illustrative Mathematics:
	 https://tasks.illustrativemathematics.org/2.OA.C
	 https://tasks.illustrativemathematics.org/2.OA.B
	ELL Overlay for Listening and Reading Grades 1 and 2 Mathematics
	ELL Overlay for Speaking and Writing for Grades 1 and 2 Mathematics
Grade Level DOK	Grade 2 Math DOK Samples
Examples	

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Unit of Ctude	I lait 6 Day 21
Unit of Study	Unit 6 - Problem Solving with Length, Money, and Data
Time Frame/Pacing	27 days
	Notes on Pacing : consider consolidating Lessons 1 and 2, Lessons 3 and 4, Lessons
	11 and 12, and Lessons 14 and 15. Consider omitting Lesson 26, or consolidate it with
	Lesson 25.
Big Ideas	Data can be modeled and used to make inferences.
Unit Essential	 How does the type of data influence the choice of display?
Questions	 How can probability and data analysis be used to make predictions?
PA Core Standards	CC.2.4.2.A.1 Measure and estimate lengths in standard units using appropriate tools.
	CC.2.4.2.A.3 Solve problems using coins and paper currency with appropriate
	symbols.
	CC.2.4.2.A.4 Represent and interpret data using line plots, picture graphs, and bar
	graphs.
	CC.2.4.2.A.6 Extend the concepts of addition and subtraction to problems involving
	length.
	CC.2.1.2.B.3 Use place value understanding and properties of operations to add and
	subtract within 1000.
Learning Objectives	 problem solve with dollars, dimes, pennies, quarters, and nickels
(Concepts Taught)	• measuring and estimating length from both the customary system and the metric
	system
	• represent data given by measurement and money data using picture graphs, bar
	graphs, and line plots
Performance	Problem Solving with Categorical Data
Objectives (Skills	• Sort and record data into a table using up to four categories; use category counts
Demonstrated)	to solve word problems.

- Draw and label a picture graph to represent data with up to four categories.
- Draw and label a bar graph to represent data; relate the count scale to the number line.
- Draw a bar graph to represent a given data set.
- Solve word problems using data presented in a bar graph.

Problem Solving with Coins and Bills

- Recognize the value of coins and count up to find their total value.
- Solve word problems involving the total value of a group of coins.
- Solve word problems involving the total value of a group of bills.
- Solve word problems involving different combinations of coins with the same total value.
- Use the fewest number of coins to make a given value.
- Use different strategies to make \$1 or make change from \$1.
- Solve word problems involving different ways to make change from \$1.
- Solve two-step word problems involving dollars or cents with totals within \$100 or \$1.

Creating an Inch Ruler

- Connect measurement with physical units by using iteration with an inch tile to measure.
- Apply concepts to create inch rulers; measure lengths using inch rulers.

Measuring and Estimating Length Using Customary and Metric Units

- Measure various objects using inch rulers and yardsticks.
- Develop estimation strategies by applying prior knowledge of length and using mental benchmarks.
- Measure an object twice using different length units and compare; relate measurement to unit size.
- Measure to compare the differences in lengths using inches, feet, and yards.

Problem Solving with Customary and Metric Units

- Solve two-digit addition and subtraction word problems involving length by using tape diagrams and writing equations to represent the problem.
- Identify unknown numbers on a number line diagram by using the distance between numbers and reference points.
- Represent two-digit sums and differences involving length by using the ruler as a number line.

Displaying Measurement Data

- Collect and record measurement data in a table; answer questions and summarize the data set.
- Draw a line plot to represent the measurement data; relate the measurement scale to the number line.
- Draw a line plot to represent a given data set; answer questions and draw conclusions based on measurement data.

Key Vocabulary

New or Recently Introduced Terms

bar graph, category, data, degree, foot, inch, legend, line plot, picture graph, scale, survey, symbol, table, thermometer, yard

Familiar Terms and Symbols

benchmark number, centimeter, cents, coins including quarter (PA Core Vocab), dime (PA Core Vocab), nickel (PA Core Vocab) and penny (PA Core Vocab), compare, compose, decompose, difference, dollars, endpoint

Assessments	Exit tickets for each lesson, Mid Module Assessment, End of Module Aggestment
	Assessment
	• Topic A quiz: https://embarc.online/mod/page/view.php?id=6851
	• Topic B quiz: https://embarc.online/mod/page/view.php?id=6852
	• Topic C and D quiz: https://embarc.online/mod/page/view.php?id=6853
	• Topic E quiz: https://embarc.online/mod/page/view.php?id=6855
	Topic F quiz: https://embarc.online/mod/page/view.php?id=6856
Authentic Examples	Application Problems
(real-world tasks)	 Lesson 5 – create own survey and collect and analyze data
	 Lesson 6-13 – solving problems using coins
	• Lesson 16 and 17 – measuring items with a ruler
Visual	• bar graph (representation of data)
Representations and	• centimeter cube
Strategies	centimeter ruler
	• dice
	• grid paper
	• inch and centimeter ruler
	• inch tiles
	• line plot
	 measuring tape
	meter stick
	money (i.e., dollars, coins)
	number bond
	• number line
	 personal white board
	picture graph
	• table
	• tape diagram
	• yardstick
Writing in Math	Mid Module Assessment question 4 (p. 125 Teacher Edition).
	End-of-Module Assessment question 4 (p. 271 Teacher Edition).
Culturally	• https://www.engageny.org/resource/grade-2-mathematics-module-7 (see the
Responsive	various language resources under "Downloadable Resources")
Activities	
Resources and	Primary Resource: Eureka Module 7
Differentiation Tools	Other Resources:
	• <u>www.zearn.org</u> (Grade 2 Mission 7)
	• 3-Act Math Tasks: https://gfletchy.com/it-all-adds-up/ ,
	https://gfletchy.com/let-it-fly/
	Problem of the Month:
	o <u>Digging Dinosaurs</u> , (Level B)
	o <u>Diminishing Return</u> ,
	 Courtney's Coin Collection
	Illustrative Mathematics:
	o https://tasks.illustrativemathematics.org/2.OA.B
	o https://tasks.illustrativemathematics.org/2.MD.A
	 https://tasks.illustrativemathematics.org/content-standards/2/MD/A/3
	https://tasks.illustrativemathematics.org/content-standards/2/MD/C/8
	• https://tasks.illustrativemathematics.org/2.MD.D

	ELL Overlay for Listening and Reading Grades 1 and 2 Mathematics
	ELL Overlay for Speaking and Writing for Grades 1 and 2 Mathematics
Grade Level DOK	Grade 2 Math DOK Samples
Examples	

Course Summary: Grade 2 mathematics is about (1) extending understanding of base-ten notation; (2) building fluency with addition and subtraction; (3) using standard units of measure; and (4) describing and analyzing shapes.

- 1. Make sense of problems and persevere in solving them.
 - 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
 - 4. Model with mathematics.
 - 5. Use appropriate tools strategically.
 - 6. Attend to precision.
 - 7. Look for and make use of structure.
- 8. Look for and makes sense of regularity in repeated reasoning.

Unit of Ctudy	I Init 7 The state of the state
Unit of Study	Unit 7 - Time, Shapes, and Fractions as Equal Parts of Shapes
Time Frame/Pacing	19 days
	Notes on Pacing: consider consolidating Lessons 9 and 10
Big Ideas	Geometric relationships can be described, analyzed, and classified based on spatial
	reasoning and/or visualization.
Unit Essential	How are spatial relationships, including shape and dimension, used to draw,
Questions	construct, model, and represent real situations or solve problems?
	 How can the application of the attributes of geometric shapes support
	mathematical reasoning and problem solving?
	How can geometric properties and theorems be used to describe, model, and
	analyze situations?
PA Core Standards	CC.2.3.2.A.1 Analyze and draw two- and three dimensional shapes having specified
	attributes.
	CC.2.3.2.A.2 Use the understanding of fractions to partition shapes into halves,
	quarters, and thirds.
	CC.2.4.2.A.2 Tell and write time to the nearest five minutes using both analog and
	digital clocks.
Learning Objectives	 investigate, describe, and reason about the composition and decomposition of
(Concepts Taught)	shapes to form other shapes
	 develop a foundation for understanding area, volume, congruence, similarity,
	and symmetry through building, drawing, and analyzing two- and
	three-dimensional shapes
Performance	Attributes of Geometric Shapes
Objectives (Skills	 Describe two-dimensional shapes based on attributes.
Demonstrated)	 Build, identify, and analyze two-dimensional shapes with specified attributes.

• Use attributes to draw different polygons quadrilaterals, pentagons, and hexagons. • Use attributes to identify and draw different quadrilaterals including rectangles, rhombuses, parallelograms, and trapezoids. • Relate the square to the cube, and describe the cube based on attributes. **Composite Shapes and Fraction Concepts** • Combine shapes to create a composite shape; create a new shape from composite shapes. • Interpret equal shares in composite shapes as halves, thirds, and fourths. Halves, Thirds, and Fourths of Circles and Rectangles • Partition circles and rectangles into equal parts, and describe those parts as halves, thirds, or fourths. • Describe a whole by the number of equal parts including 2 halves, 3 thirds, and 4 fourths. • Recognize that equal parts of an identical rectangle can have different shapes. **Application of Fractions to Tell Time** • Construct a paper clock by partitioning a circle into halves and quarters, and tell time to the half hour • Tell time to the nearest five minutes. • Tell time to the nearest five minutes; relate a.m. and p.m. to time of day. • Solve elapsed time problems involving whole hours and a half hour. **Key Vocabulary New or Recently Introduced Terms** a.m./p.m., analog clock, angle, parallel, parallelogram, partition, pentagon, polygon, quadrilateral, quarter past, quarter to/until, right angle, third of/thirds, whole **Familiar Terms and Symbols** attributes, cubes, digital clock, face, fourth of/fourths, half of/halves, half past, hour, minute, o'clock, quarter of/quarters, tangram, two-dimensional shapes, cube, circle, half-circle, hexagon, quarter-circle, rectangle, rhombus, square, trapezoid, triangle Assessments • Exit Tickets for each lesson, Mid Module Assessment, End of Module Assessment • Topic A quiz: https://docs.google.com/document/d/1cD7j6OLMVeDkMzXXxxLsbedNhtXTT 8ew90WVik-xEBM/edit?usp=sharing • Topic B quiz: https://docs.google.com/document/d/16Wj3OFpR0XIc6o_gfgfS3xtZrhrEBp-U RsNQhaycXns/edit?usp=sharing • Topic C and D quiz: https://docs.google.com/document/d/1hivWDFBc3xOjxLHuhCzt9xroilF7iwMl 5kc0hxKDpzY/edit?usp=sharing • Topic E quiz: https://docs.google.com/document/d/1q6XYmqMsZo3Dkg8D7NsjWaSNCXbf NF1WtMWQo0cgCaA/edit?usp=sharing • Topic F quiz: https://docs.google.com/document/d/1Km5c-hXM1eKN7-bnZAJkI1chm_w0gI UVyfuVmXbS9sU/edit

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Authentic Examples	Application Problems
(real-world tasks)	• Lessons 13-16 – concepts of time on an analog clock
Visual	• Cube: a three-dimensional shape (real-world examples such as a die, alphabet
Representations and	blocks, or a box)
Strategies	 Geoboards
C	Large instructional geared clock
	Pattern blocks
	Personal white boards
	• Rulers
	• Spaghetti
	 Student clocks, preferably those with gears that can provide the appropriate
	hour-hand alignment
	Tangrams
XX7 *4* * 3.45 43	• Toothpicks
Writing in Math	Mid Module Assessment question 4 (p. 189 Teacher Edition).
Culturally	• <u>https://www.engageny.org/resource/grade-2-mathematics-module-8</u> (see the
Responsive	various language resources under "Downloadable Resources")
Activities	• https://learnenglishkids.britishcouncil.org/short-stories/one-moment-around-the-world
	What time is it in different parts of the world? Includes military time
	• https://www.slideshare.net/geetasngh/history-of-time-powerpoint-presentations-for-kid
	<u>S</u>
	History of clocks
Resources and	Primary Resource: Eureka Module 8
Differentiation Tools	Other Resources:
	• www.zearn.org (Grade 2 Mission 8)
	Problem of the Month
	o The Shape of Things, (Level A)
	Once Upon a Time, (Level A and B)
	o Tri-Triangles (Level A and B)
	• Illustrative Mathematics:
	• https://tasks.illustrativemathematics.org/2.OA.B
	• https://tasks.illustrativemathematics.org/content-standards/2/MD/C/7
	• https://tasks.illustrativemathematics.org/2.G
	ELL Overlay for Listening and Reading Grades 1 and 2 Mathematics
	ELL Overlay for Speaking and Writing for Grades 1 and 2 Mathematics
Grade Level DOK	Grade 2 Math DOK Samples
Examples	Of auc 2 Main DOIX Sampies
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The following link takes you to the academic vocabulary list.

General Academic Vocabulary

Course Summary: Grade 2 mathematics is about (1) extending understanding of base-ten notation; (2) building fluency with addition and subtraction; (3) using standard units of measure; and (4) describing and analyzing shapes.

- 1. Make sense of problems and persevere in solving them.
 - 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
 - 4. Model with mathematics.
 - 5. Use appropriate tools strategically.
 - 6. Attend to precision.
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Unit of Study	Unit 8 - Addition and Subtraction Within 1,000 with Word Problems to 100
Time Frame/Pacing	23 days
	Notes on Pacing: None for this module
Big Ideas	Mathematical relationships can be represented as expressions, equations, and
	inequalities in mathematical situations.
Unit Essential	How are relationships represented mathematically?
Questions	How can expressions, equations, and inequalities be used to quantify, solve,
	model and/or analyze mathematical situations?
PA Core Standards	CC.2.1.2.B.3 Use place value understanding and properties of operations to add and
	subtract within 1000.
Learning Objectives	 place value strategies, manipulatives, and math drawings to extend their
(Concepts Taught)	conceptual understanding of the addition and subtraction algorithms to numbers
	within 1,000
	• maintain addition and subtraction fluency within 100 through daily application
	work to solve one- and two-step word problems of all types
	 use place value reasoning to explain why their addition and subtraction
	strategies work
Performance	Strategies for Adding and Subtracting Within 1,000
Objectives (Skills	• Relate 10 more, 10 less, 100 more, and 100 less to addition and subtraction of
Demonstrated)	10 and 100.
	 Add and subtract multiples of 100, including counting on to subtract.
	• Add multiples of 100 and some tens within 1,000.

	• Subtract multiples of 100 and some tone within 1 000
	Subtract multiples of 100 and some tens within 1,000. Use the aggregative property to make a bundled in one added.
	Use the associative property to make a hundred in one addend. Use the associative property to subtract from three digit name and varify.
	• Use the associative property to subtract from three-digit numbers and verify solutions with addition.
	Share and critique solution strategies for varied addition and subtraction problems within 1,000.
	problems within 1,000. Strategies for Composing Tens and Hundreds Within 1,000
	Relate manipulative representations to the addition algorithm.
	Use math drawings to represent additions with up to two compositions and
	relate drawings to the addition algorithm.
	Choose and explain solution strategies and record with a written addition
	method.
	Strategies for Decomposing Tens and Hundreds Within 1,000
	Relate manipulative representations to the subtraction algorithm, and use
	addition to explain why the subtraction method works.
	• Use math drawings to represent subtraction with up to two decompositions,
	relate drawings to the algorithm, and use addition to explain why the subtraction
	method works.
	• Subtract from multiples of 100 and from numbers with zero in the tens place.
	• Apply and explain alternate methods for subtracting from multiples of 100 and
	from numbers with zero in the tens place.
	Student Explanations for Choice of Solution Methods
	Choose and explain solution strategies and record with a written addition or
	subtraction method.
Key Vocabulary	New or Recently Introduced Terms
	compensation
	Familiar Terms and Symbols
	addend, addition, algorithm, bundle, compose, decompose, difference, equation, new
	groups below, number bond, place value, place value chart, place value or number disk,
	rename, simplifying strategy, subtraction, tape diagram, total, unbundle, units of ones/tens/hundreds
Assessments	Exit Tickets for each lesson, Mid Module Assessment, and End of Module
Assessments	Assessment
	Topic A quiz: https://embarc.online/mod/page/view.php?id=6802
	Topic B quiz: https://embarc.online/mod/page/view.php?id=6803
	Topic C quiz: https://embarc.online/mod/page/view.php?id=6804
	Topic D quiz: https://embarc.online/mod/page/view.php?id=6805
Authentic Examples	Application Problems
(real-world tasks)	
Visual	Arrow notation, arrow way
Representations and	Chip model
Strategies	Hide Zero cards
	Number Bonds
	• Whiteboards
	Place value disks
	Place value charts
Ì	l Tr 1'
Writing in Math	 Tape diagram Mid-Module Assessment Problem e (p. 117 Teacher Edition).

Culturally	• https://www.engageny.org/resource/grade-2-mathematics-module-5 (see the
Responsive	various language resources under "Downloadable Resources")
Activities	,
Resources and	Primary Resource: Eureka Module 5
Differentiation Tools	Other Resources:
	• <u>www.zearn.org</u> (Grade 2 Mission 5)
	• 3-Act Math Tasks: https://gfletchy.com/downsizing-tomatoes/
	• Problem of the Month:
	• http://www.insidemathematics.org/assets/problems-of-the-month/double
	%20down.pdf,(Level B)
	• http://www.insidemathematics.org/assets/problems-of-the-month/got%2
	<pre>Oyour%20number.pdf, (Level D and E)</pre>
	• Illustrative Mathematics:
	 https://tasks.illustrativemathematics.org/2.OA.B
	 https://tasks.illustrativemathematics.org/2.NBT.A
	ELL Overlay for Listening and Reading Grades 1 and 2 Mathematics
	ELL Overlay for Speaking and Writing for Grades 1 and 2 Mathematics
Grade Level DOK	Grade 2 Math DOK Samples
Examples	